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Abstract. We consider an optical beam propagated through the atmosphere and incident on an object causing a temperature rise. In clear air, the physical characteristics of the optical beam transmitted to the object surface are influenced primarily by the effect of atmospheric turbulence, which can be significant near the ground or ocean surface. We use a statistical model to quantify the expected power transfer through turbulent atmosphere and provide guidance toward the threshold of thermal blooming for the considered scenarios. The bulk thermal characteristics of the materials considered are used in a thermal diffusion model to determine the net temperature rise at the object surface due to the incident optical beam. These results of the study are presented in graphical form and are of particular interest to operators of high power laser systems operating over large distances through the atmosphere. Numerical examples include a CO₂ laser ($\lambda = 10.6 \mu\text{m}$) with: aperture size of 5 cm, varied pulse duration, and propagation distance of 0.5 km incident on 0.1-mm copper, 10-mm polyimide, 1-mm water, and 10-mm glass/resin composite targets. To assess the effect of near ground/ocean laser propagation, we compare turbulent (of varying degrees) and nonturbulent atmosphere. © The Authors. Published by SPIE under a Creative Commons Attribution 3.0 Unported License. Distribution or reproduction of this work in whole or in part requires full attribution of the original publication, including its DOI. [DOI: [10.1117/1.OE.52.3.036001](https://doi.org/10.1117/1.OE.52.3.036001)]

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1 Introduction

When a high-power optical beam is propagated through atmospheric turbulence, and is incident on an object, power is transferred, causing the temperature of the object to rise. Recent demonstrations by the Navy show a multikilowatt beam igniting the engine housing of a small boat from over 1-km distance in a maritime environment.¹ Interest in this technology motivates the investigation of turbulence effects on beam-wave propagation and its impact on target heating. Laser beam propagation through the atmosphere in the presence of turbulence has been studied extensively.^{2,3} The Navy has developed high energy laser code for atmospheric propagation, a 3-D code to model high energy laser propagation, and has published many papers based on the results.⁴⁻⁶ The basic problem of laser-induced heating of a variety of solid objects has been studied.⁷⁻⁹ Many studies of laser heating until now have been performed in the context of laser machining, without regard to a large volume of turbulent media between the transmitter and solid object. While these studies give useful results for the laser power and dwell times common in laser machining, these parameters do not generally translate well to the problem of a laser beam propagated over a large distance through the atmosphere. In these cases, spot sizes are generally larger and dwell times generally longer. This paper provides a prediction of temperature rise due to a high power optical emitter operating over a large distance in a variety of plausible atmospheric conditions.

To predict heating of solid objects due to the incident laser, beam-wave propagation, optical absorption, and heat diffusion are simultaneously considered. For a beam wave in turbulence, a statistical model is used to obtain the second moment, which is the long-term, average intensity. For short pulse durations, on the order of 10 ms or less, the fourth-order moment is also obtained. A beam of sufficiently high-power density causes heating of the atmosphere and nonlinear propagation, or thermal blooming, of the beam. The threshold transmit powers, beyond which thermal blooming has a discernible effect on the characteristics of the optical beam, are readily estimated for each considered scenario. A discussion of possible implications of exceeding this threshold follows.

For transmit powers below the threshold, thermal blooming effects are disregarded. The beam wave is incident on the object, and power is absorbed, causing a net heating of the material. To quantify the absorbed power the optical absorptivity of the object must be determined. We assume optical absorption in the form of intrinsic bulk absorption. For metallic objects, a Drude model is used to find the complex dielectric constant of the object at the desired optical frequency. For nonmetals, published optical absorptance values are used. The net temperature rise at the object surface is calculated using a thermal diffusion model, appropriate boundary conditions, and the bulk thermal characteristics of the target material. A flow chart of the process is provided in Fig. 1.

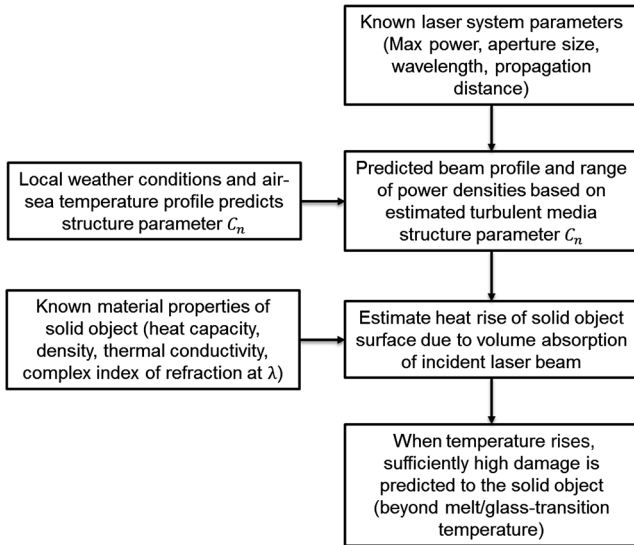


Fig. 1 Flow chart of laser heating of solid object through turbulence calculation.

2 Focused Beam in Atmospheric Turbulence

The expression for an optical focused beam in free space, as shown in Fig. 2, is given by Ref. 10.

$$U_0(\rho, z) = \frac{A_0}{(1 + i\xi z)} \exp \left[ikz - \left(\frac{k\xi}{2} \right) \frac{\rho^2}{(1 + i\xi z)} \right], \quad (1)$$

where ξ is given by

$$\xi = \xi_1 + i\xi_2 = \frac{1}{z_0} + i \frac{1}{R_0}. \quad (2)$$

Variable z_0 is called the ‘‘Rayleigh range,’’ and gives an approximate dividing distance such that the field is considered in the ‘‘near field’’ for $z < z_0$. The Rayleigh range is a function of wavenumber k and aperture radius W_0 :

$$z_0 = \frac{kW_0^2}{2}. \quad (3)$$

R_0 is the focal distance. The field at $z = 0$ has Gaussian amplitude and a focused phase front. Figure 1 shows the focused beam in atmospheric turbulence and a target. We define the total input power at $z = 0$, and amplitude constant A_0 as follows:

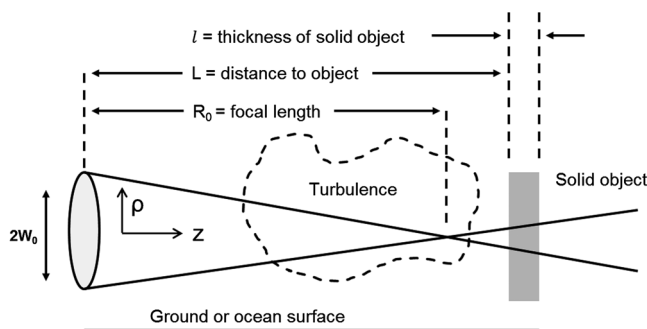


Fig. 2 Focused beam and object.

$$P_t = \left(\frac{\pi}{2} W_0^2 \right) A_0^2 \quad (4)$$

$$A_0^2 = \frac{|E|^2}{2\eta_0}. \quad (5)$$

The intensity distribution of a focused beam in the turbulence has been obtained, and in the range $z_i \gg z \gg z_c$, where z_i and z_c depend on the inner scale l_0 and outer scale L_0 of the turbulence as follows:

$$z_i = (0.39C_n^2 k^2 l_0^{5/3})^{-1} \quad (6)$$

$$z_c = (0.39C_n^2 k^2 L_0^{5/3})^{-1}. \quad (7)$$

The intensity distribution is given by Refs. 10 and 11:

$$I(\rho_c, z) = A_0^2 \frac{2W_0^2}{W^2} \exp(-\alpha_E z) \int_0^\infty t J_0(t\rho') \times \exp \left[-t^2 - \left(\frac{1}{2} \right) D_s t^{5/3} \right] dt, \quad (8)$$

where $\rho' = (2\sqrt{2})\rho_c/W$; α_E is the atmospheric attenuation constant. The structure function D_s and beam size W are given by

$$D_s = 6.2C_n^2 k^{1/3} z^{8/5} W^{-5/3}. \quad (9)$$

$$W^2 = W_0^2 [(\xi_1 z)^2 + (1 - \xi_2 z)^2]. \quad (10)$$

The atmospheric attenuation constant α_E accounts for the absorption and scattering properties of the medium. Values for α_E are widely known and reduction of laser transmittance due to atmospheric attenuation for distances < 1 km in relatively clear air is minimal.¹² In the numerical calculations that follow, $\alpha_E = 0$ is assumed unless otherwise specified.

The index of refraction structure constant C_n^2 has been found in the range 10^{-17} (very weak) to 10^{-12} (very strong) over land, and 10^{-16} (weak) to 10^{-13} (strong) over the open ocean.^{11,13} The coherent intensity of the beam wave is given by Ref. 10:

$$|U|^2 = \frac{W_0^2}{W^2} \exp \left(-\frac{2\rho^2}{W^2} - 2\alpha_0 z \right), \quad (11)$$

where the constant of attenuation due to turbulence α_0 is

$$\alpha_0 = 0.39C_n^2 k^2 L_0^{5/3}. \quad (12)$$

These expressions can be used to model the intensity of an optical beam through turbulence at the location of a distant target.

3 Short-Term Intensity

For a short term, on the order of 10 ms or less, the peak intensity is approximately close to the speckle intensity. In this context, speckle refers to the amplitude variations in the laser spot caused by constructive/destructive interference from incident rays of varying phase. When the laser dwell time is sufficiently short, the interference pattern is

essentially static, and the use of the average intensity to determine peak intensity is not appropriate. The fourth-order intensity I^2 can be approximately given by the following, using circular complex Gaussian assumption:

$$I^2 \approx 2I^2 - |U|^4. \quad (13)$$

Under this approximation, we get short-term intensity [Eq. (14)], and when the time is not short, we use the average intensity [Eq. (15)].

$$I_{\text{short}} \approx [2I^2 - |U|^4]^{1/2}. \quad (14)$$

$$I \approx [I^2 - |U|^4]^{1/2}. \quad (15)$$

Using Eqs. (14) and (15), we can calculate the intensity of the laser beam at the object surface. In the numerical examples, Eq. (14) is used for pulse durations less than 10 ms, and Eq. (15) is used for pulse durations greater than or equal to 10 ms. This arbitrary choice of a short-pulse cutoff results in a small discontinuity in the incident flux at 10 ms.

4 Thermal Blooming in the Atmosphere

The air in the atmosphere has some absorption at optical wavelengths. The absorption of power produces local heating, thereby increasing the pressure and decreasing the density, which causes a decrease of the refractive index. The beam intensity profile is initially maximum on the axis, but as the heating occurs, the refractive index decreases on the beam axis, which causes a divergence of the beam from the beam axis. This is referred to as thermal blooming of the beam.¹⁴ Thermal blooming has been studied numerically and analytically using geometric optics, perturbation theory, and extended Huygens-Fresnel methods. If multiple pulses are used, the wind moves the minimum refractive index away from the beam axis, and the new pulse will be focused into the upstream direction of the wind and the center of the beam moves toward the axis giving enhancement of the peak power on the axis. The peak power can then become higher than the free space peak power. Numerical examples in Ref. 14 show that the peak power can be enhanced by 17%.

If we make a few assumptions about the conditions of operation, we can use an order-of-magnitude expression, following the lead of Ref. 14, to estimate the onset of thermal blooming effects. We first assume the beam wave is propagated through some transverse flow of velocity v , and that the air has some absorption coefficient α , which contributes to local heating of the propagation medium. From Ref. 14 we can estimate the minimum transmit power level at which thermal blooming effects may be significant:

$$P_{\text{min}} \approx \frac{\rho_0 \lambda \gamma \pi v W_0}{\alpha_E L (\gamma - 1) (n_0 - 1)}. \quad (16)$$

If we assume the following constants (typical values for sea level air): γ is the heat capacity ratio; $\gamma = 1.4$ for air at 20°C; n_0 is the initial index of refraction; $(n_0 - 1) = 3 \times 10^{-4}$ for air; ρ_0 is the ambient pressure; $\rho_0 = 10^5 \text{ Nm}^{-2}$ at sea level; α_E is the atmospheric extinction coefficient; $\alpha_E = 4 \times 10^{-4} \text{ m}^{-1}$ for tropical air in rural environment;¹⁰ λ is the wavelength of radiation; $\lambda = 10^{-5} \text{ m}$; v is the velocity of

the transverse flow; $v = 13.6 \text{ ms}^{-1}$ about 30 mph; W_0 is the radius of the aperture; $W_0 = 0.05 \text{ m}$; and L is the propagation distance to the target; $L = 0.5 \times 10^3 \text{ m}$, then we find that the threshold power is approximately

$$P_{\text{min}} \approx (2.9 \times 10^7) \frac{\pi v W_0}{L} \approx 120 \text{ kW}.$$

The order-of-magnitude calculation shows that for the power densities considered in this analysis, it requires transmit power in excess of the upper limit of most CO₂ laser systems to encounter thermal blooming effects. Additionally, this calculation did not consider the effect of atmospheric turbulence, which will, in general, further reduce the radiation power density along the path of the beam wave.

5 Absorbed Power in the Object

An optical beam is incident on the object and power is dissipated into the medium as heat, which will raise the temperature. The power transmitted into the object L_a can be calculated as

$$L_a = \frac{\omega \epsilon_0 \epsilon''}{2} |E_t|^2 = L_{a0} \exp(-\alpha_2 z_2). \quad (17)$$

A detailed proof comparing Eq. (17) to a widely used expression for total absorbed energy based on reflected power and conservation of energy is given in the [Appendix](#).

The dielectric constant of the object is $\epsilon(\omega) = \epsilon' + i\epsilon''$ and the attenuation in the object is given by

$$\alpha_2 = 2\text{Im}(k_2), \quad (18)$$

where $k_2 = \omega \sqrt{\mu \epsilon}$.

The transmitted electric field into the object at a distance z_2 from the incident surface is given by

$$E_t(z_2) = TE_i \exp(ik_2 z_2), \quad (19)$$

where T is the transmission coefficient. If we consider a metallic object, the dielectric constant at optical wavelengths is given by a Drude model:

$$\epsilon(\omega) = 1 - \frac{\omega_p^2}{\omega \left(\omega + i \frac{1}{\tau} \right)}, \quad (20)$$

where ω_p is the plasma frequency and τ is the relaxation time. For copper, the plasma frequency and relaxation time were determined in Refs. 15–17. Using the most recent number, the value of ϵ is computed as

$$\epsilon_{\text{copper}} = -8.04 \times 10^3 + i1.85 \times 10^3. \quad (21)$$

For many nonmetals, the optical constants in the mid-infrared have been directly observed. The relative permittivity of water at 10.6 μm has been determined.¹⁸

$$\epsilon_{\text{water}} = 1.21 + i0.02. \quad (22)$$

The complex index of refraction of polyimide at 10.6 μm has been published; from this the relative permittivity is computed as follows:¹⁹

$$\epsilon_{PI} = 3.23 + i0.18. \tag{23}$$

Glass-fiber reinforced plastic (GFRP) is a mixture of glass fibers in a thermally cured plastic resin (e.g., polyesters) background material. Properties of GFRP, including volume fraction of glass fiber, melting temperature of resin, and typical thermal properties are described in Ref. 20. The complex index of refraction of silica glass at 10.6 μm has been published; from this, the relative permittivity is computed as follows:²¹

$$\epsilon_{glass} = 3.75 + i2.0. \tag{24}$$

The complex index of refraction of polyethylene at 10.6 μm has been published; from this the relative permittivity is computed as follows:²²

$$\epsilon_{PE} = 2.25 + i0.0025. \tag{25}$$

The dielectric properties of composite materials such as GFRP have been studied extensively at microwave frequencies using different mixing formulas.²³ At 10.6 μm, the size of glass inclusions in polymer resin background material are usually much larger than the wavelength, and these mixing formulas may not be applicable. Therefore, in this paper, we use a simple average of Eqs. (24) and (25) to obtain a rough estimate of the GFRP permittivity.

6 Heat Diffusion in Solid Objects

The absorbed power is given by Eq. (18), which will be the heat source for the temperature rise. The diffusion equation for the temperature is given by

$$\frac{\partial T}{\partial t} = D\nabla^2 T + \frac{L_a}{\rho C_s}, \tag{26}$$

where T is the temperature, ρ (kg/m³) is the density, C_s (J/kg°C) is the specific heat of the solid, and D (m²/s) is the thermal diffusivity. The thermal properties for the four materials under consideration are summarized in Table 1.

Equation (26) needs to be solved with boundary conditions. A commonly used approximate boundary condition is the Neumann condition:

$$\frac{\partial T}{\partial n} = 0. \tag{27}$$

This is equivalent to zero heat flow across the boundary. This boundary condition is appropriate when the heat

transfer from the solid object to the surrounding media is low (i.e., a relatively good thermal conductor in still air). The thermal time constant τ_δ for a skin depth δ_s determines the approximate time required for heat generated by the conversion of laser energy in the skin depth region to diffuse a distance greater than the thickness of the skin-depth region.

$$\delta_s = \frac{1}{\alpha_2} \tag{28}$$

$$\tau_\delta = \frac{\delta_s^2}{D} \tag{29}$$

If the laser is incident on the target for a short time relative to the skin depth of the material the heat diffusion will be approximately given as follows:²⁵

When t is in the range ($t \leq \tau_\delta$):

$$\Delta T(0, t) \approx \frac{L_a t}{\rho C_s}. \tag{30}$$

Assuming heat has diffused out of the skin depth region, for relatively short times the heat will have not yet diffused far enough to reach the back surface of the metallic object located at $z_2 = l$. This time is determined by the thermal time constant as follows:

$$\tau_l = \frac{l^2}{D}. \tag{31}$$

In this time interval heat diffuses as it would in a semi-infinite metallic object, and a Neumann boundary condition is assumed at $z_2 = 0$ only. With this assumption, the temperature rise, ΔT , at $z_2 = 0$ is given by the following expression.²⁵

When t is in the range [$\tau_\delta \ll t \leq (\tau_l/3)$]:

$$\Delta T(0, t) \approx \left(\frac{2\delta_s L_a}{\rho C_s l} \right) \left(\frac{\tau_l t}{\pi} \right)^{1/2}. \tag{32}$$

For relatively long times, the heat will have diffused through the thickness of the object, and a Neumann boundary condition assumed at both $z_2 = 0$ and $z_2 = l$. With these assumptions, the temperature rise, ΔT , at $z_2 = 0$ is given by the following expression.²⁵

Table 1 Thermal properties of various laser targets.

Material	Density (kg/m ³)	Specific heat capacity (J/kg°C)	Thermal diffusivity (m ² /s)	Skin depth thermal time constant (s)	Slab thickness thermal time constant (s)
Copper	8.92 × 10 ³	0.39 × 10 ³	1.12 × 10 ⁻⁴	7.6 × 10 ⁻¹³	2.9 × 10 ⁻⁵
Water	1.00 × 10 ³	4.18 × 10 ³	1.44 × 10 ⁻⁷	6.0 × 10 ⁻²	2.3
Polyimide ²⁴	1.42 × 10 ³	1.09 × 10 ³	7.75 × 10 ⁻⁸	9.0 × 10 ⁻⁴	1.1 × 10 ²
Glass/resin composite ²⁰	1.90 × 10 ³	1.00 × 10 ³	3.20 × 10 ⁻⁷	2.8 × 10 ⁻⁵	1.1 × 10 ²

When t is in the range $[(\tau_l/3) \leq t]$,

$$\Delta T(0, t) \approx \left(\frac{\delta_s L_a}{\rho C_s l} \right) \left(t + \frac{\tau_l}{3} \right). \quad (33)$$

7 Numerical Examples

7.1 Attenuation Due to Turbulence

We consider a beam focused on a solid copper object of thickness $l = 0.1$ mm. Figure 3 shows the predicted minimum laser dwell time required to heat the surface of the copper target to the melting point of copper using $10.6\text{-}\mu\text{m}$ radiation through a focused 5-cm aperture at 0.5 km. Although in practice it may be difficult to focus a laser at a distance of 0.5 km, we use the focused case to illustrate the worst-case degradation due to turbulence. The effect of turbulence on a collimated beam is less pronounced, and thus, the result will be closer to the free-space solution. The transmit power is varied from 10 to 100 kW, and various cases of atmospheric turbulence are considered: free space (no turbulence) and turbulence C_n^2 equal to 10^{-14} , 10^{-13} , and 10^{-12} . For the thickness of copper and time range considered, Eq. (33) is used exclusively as heat has diffused a distance much greater than the thickness of the copper target.

The plot in Fig. 3 can be used to predict the laser dwell time required to realize the onset of melting for a laser system of known transmit power. This result considers only when the absorbed power is sufficient to cause a sustained rise in temperature in excess of the melt temperature it applies generally to either pulsed or continuous wave (CW) operation, provided that the average power is held constant (e.g., 10 to 100 kW). In pulsed operation, the beam will have a higher power density, and thus, may cause a momentary spike in local temperature above the melt temperature, but during the off portion of the duty cycle the heat will diffuse out of the area and the temperature will decrease. Over many pulses the average temperature will rise at the same rate as a CW laser of equal average power.

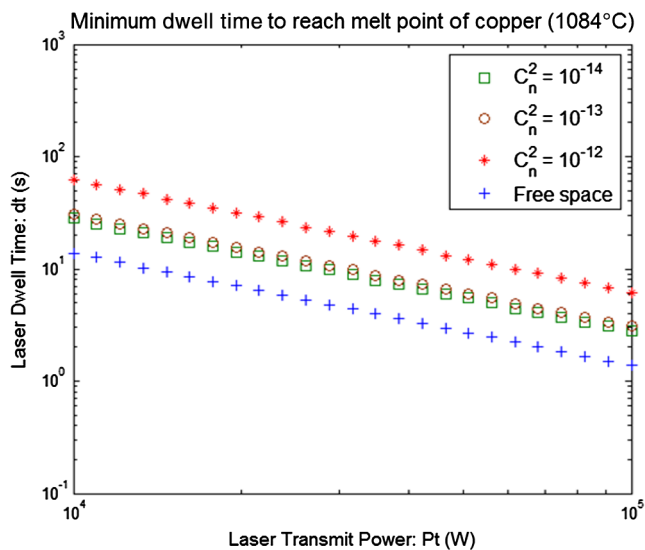


Fig. 3 ΔT versus transmit power (Pt) at $\lambda = 10.6 \mu\text{m}$; $L = 0.5$ km; $A_0 = 5$ cm (focused); $P_t = 10$ to 100 kW; copper thickness $l = 0.1$ mm.

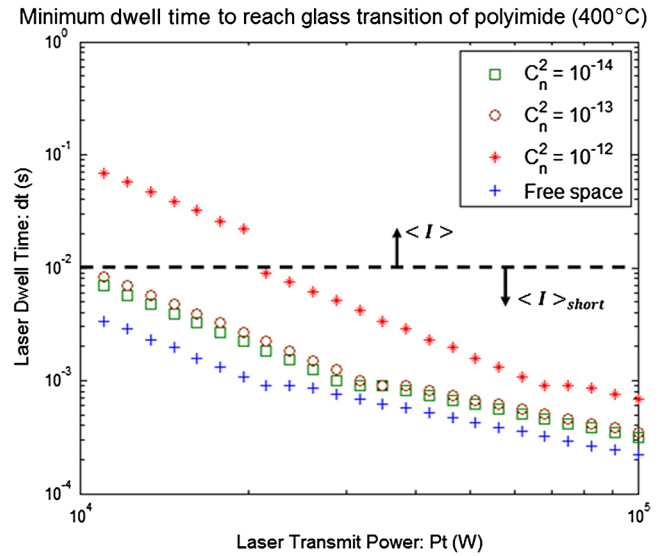


Fig. 4 ΔT versus transmit power (Pt) at $\lambda = 10.6 \mu\text{m}$; $L = 0.5$ km; $A_0 = 5$ cm (focused); $P_t = 10$ to 100 kW; Kapton thickness $l = 10$ mm.

Figure 4 shows the predicted minimum laser dwell time required to heat the surface of a $l = 10$ mm sample of Kapton (polyimide) target the glass transition temperature (400°C) using $10.6\text{-}\mu\text{m}$ radiation through a focused 5-cm aperture at 0.5 km. The transmit power is varied from 10 to 100 kW, and various cases of atmospheric turbulence are considered: free space (no turbulence) and turbulence C_n^2 equal to 10^{-14} , 10^{-13} , and 10^{-12} . The discontinuity at $dt = 10^{-2}$ s is due to the inclusion of the fourth-order moment for short pulse durations as described in Sec. 3. For the thickness of polyimide and time range considered, Eq. (30) is used for $t < 9 \times 10^{-4}$ s, and Eq. (32) is used for $t > 9 \times 10^{-4}$ s.

Figure 5 shows the predicted minimum laser dwell time required to heat the surface of a $l = 1$ mm sample of water to its boiling point (100°C) using $10.6\text{-}\mu\text{m}$ radiation through

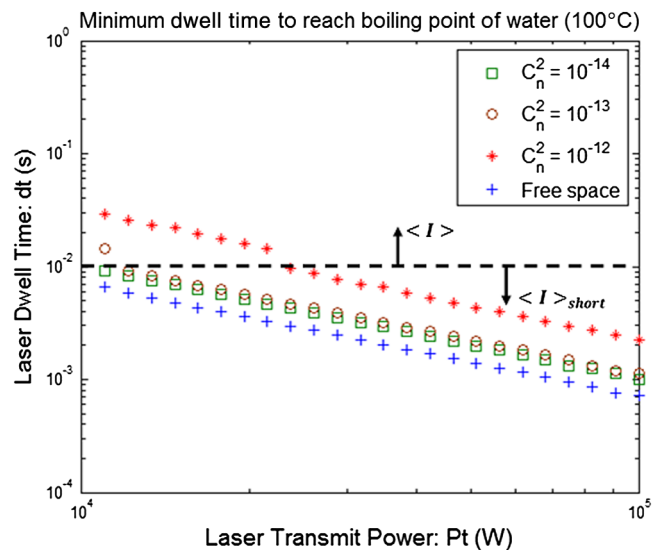


Fig. 5 ΔT versus transmit power (Pt) at $\lambda = 10.6 \mu\text{m}$; $L = 0.5$ km; $A_0 = 5$ cm (focused); $P_t = 10$ to 100 kW; water thickness $l = 1$ mm.

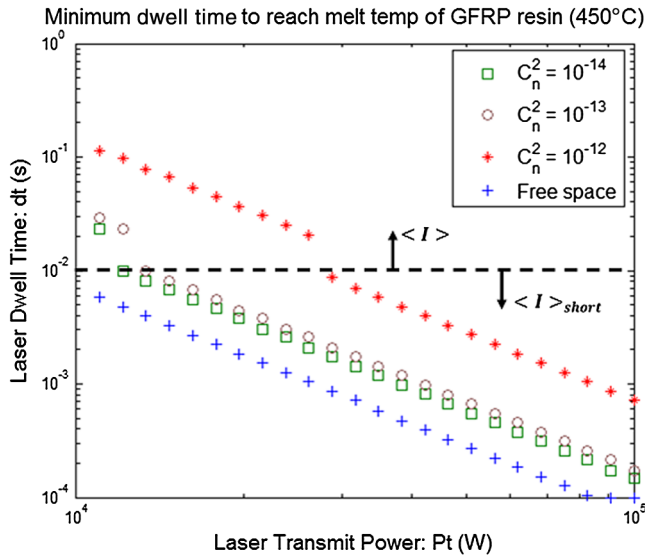


Fig. 6 ΔT versus transmit power (P_t) at $\lambda = 10.6 \mu\text{m}$; $L = 0.5 \text{ km}$; $A_0 = 5 \text{ cm}$ (focused); $P_t = 10$ to 100 kW ; glass-fiber reinforced plastic (GFRP) thickness $l = 10 \text{ mm}$.

a focused 5-cm aperture at 0.5 km. The transmit power is varied from 10 to 100 kW, and various cases of atmospheric turbulence are considered: free space (no turbulence) and turbulence C_n^2 equal to 10^{-14} , 10^{-13} , and 10^{-12} . For the thickness of water and power ranges range considered, Eq. (30) is used exclusively as $\tau_\delta = 0.06 \text{ s}$, which is greater than the maximum required laser dwell time to heat water to its boiling point.

Figure 6 shows the predicted minimum laser dwell time required to heat the surface of a $l = 10 \text{ mm}$ sample of GFRP to the melting point of polyester resin using $10.6\text{-}\mu\text{m}$ radiation through a focused 5-cm aperture at 0.5 km. The transmit power is varied from 10 to 100 kW, and various cases of atmospheric turbulence are considered: free space (no turbulence) and turbulence C_n^2 equal to 10^{-14} , 10^{-13} , and 10^{-12} . For the thickness of GFRP and power ranges range considered, Eq. (32) is used exclusively as the required laser dwell times fall between $\tau_\delta = 2.8 \times 10^{-5} \text{ s}$ and $(\tau_l/3) = 1.1 \times 10^2 \text{ s}$.

7.2 Attenuation Due to Turbulence and Atmospheric Extinction

The combined effect of atmospheric scattering and attenuation on a laser beam propagated through the atmosphere to a solid object target is a reduction in transmittance, which can, under the right conditions, become similar to or even greater in magnitude than the interference caused by atmospheric turbulence. Like the attenuation caused by atmospheric turbulence, the total extinction seen in a volume of atmosphere increases with the greater separation between the laser source and the target. This is easily deduced from Eq. (8), which contains the exponential attenuation term, $\exp(-\alpha_E z)$. The product of extinction coefficient and linear distance is commonly called optical thickness: $\tau_E = \alpha_E z$. An order-of-magnitude approximation is that the effect of atmospheric extinction should be considered when optical thickness $\tau_E \gtrsim 1$. For a distance of 0.5 km this corresponds to $\alpha_E \gtrsim 2 \text{ km}^{-1}$. Figure 7 shows the effect of atmospheric

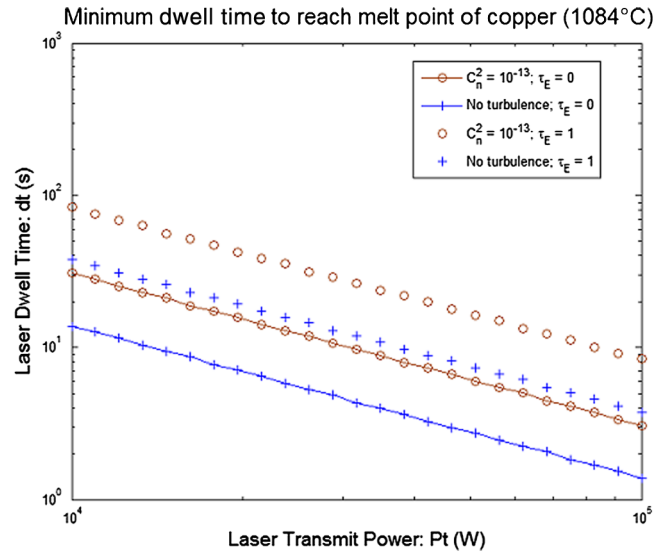


Fig. 7 ΔT versus transmit power (P_t) at $\lambda = 10.6 \mu\text{m}$; $L = 0.5 \text{ km}$; $A_0 = 5 \text{ cm}$ (focused); $P_t = 10$ to 100 kW ; copper thickness $l = 0.1 \text{ mm}$.

extinction in this range on the laser dwell time required to heat a copper target to its melting point. Considering the free space (no turbulence) case, we can observe an increase in minimum laser dwell time when $\alpha_E = 2 \text{ km}^{-1}$, which is in the range of the increase required in moderate turbulence. If optical thickness $\tau_E \ll 1$, then the increase in laser dwell time will be minimal, and if $\tau_E \gg 1$, then the effect of atmospheric extinction will dominate, and the relative effect of turbulence will be small.

Figure 7 shows the effect of $\alpha_E = 2 \text{ km}^{-1}$ on laser propagation over 500 m. In real-world conditions, this value of atmospheric extinction is not typical when visibility is relatively good. According to Ref. 13, for visibility ranging from hazy to clear (5 to 40 km) atmospheric extinction remains below $\alpha_E = 0.33 \text{ km}^{-1}$ in a rural nonmaritime environment. According to Ref. 26, the atmospheric extinction coefficient for a maritime environment at 99% relative humidity is $\alpha_E = 0.45 \text{ km}^{-1}$. In the presence of fog, however, when visibility can be reduced to 50 to 1000 m atmospheric extinction in the range $\alpha_E = 1 - 100 \text{ km}^{-1}$ can be expected. This is shown in a number of fog model calculations in Refs. 26 and 27.

8 Conclusions

This paper presents a study on an optical beam propagated through turbulence and incident on various targets, generating heat and causing a temperature rise. The propagation of a beam wave in the atmosphere is discussed, including the fourth-order moment and the effect of thermal blooming. Transmitted power of 10 to 100 kW is absorbed in the target and converted into heat causing the temperature to rise. Numerical examples are given for $10.6 \mu\text{m}$, free-space, and turbulence, aperture size $W_0 = 5 \text{ cm}$, copper target thickness of 0.1 mm, Kapton target thickness of 0.1 mm, water thickness of 1 mm, and GFRP thickness of 10 mm. In each case, the beam is focused at 0.5 km, and the minimum laser dwell time required to heat the sample to its melting/boiling point is predicted. The effect of atmospheric extinction through absorption and scattering is discussed, and it is determined

that the attenuation due to atmospheric extinction should be included in a dwell time calculation when $\tau_E \gtrsim 1$. A plot is presented which shows the predicted difference in required dwell time for a focused laser through the atmosphere in zero and moderate turbulence with $\tau_E = 0$ and $\tau_E = 1$.

Appendix: Proof for Absorbed Power Equation

The absorbed power-per-unit volume in the solid object target is given in Eq. (16). Likewise, the total absorbed power from $z = 0$ to $z = d$ is given by

$$\int_0^d L_a dz. \quad (34)$$

If the integration path is sufficiently large, the total power is equal to the incident power minus the reflected power. This approach has been used in several papers including Refs. 16 and 17. In the case of thin objects and/or short integration paths, Eq. (34) gives the correct absorbed power. In this paper, we consider solid copper objects, and because the skin depth is small relative to object thickness, we can use Eq. (34) with $\rightarrow \infty$. To prove equivalence, we can show that the incident power P_{inc} minus the reflected power P_{ref} is equal to Eq. (37), with $d \rightarrow \infty$.

We start with the exact formulation:

$$E_i(1 + R) = E_t \quad (35)$$

$$\frac{E_i}{Z_0}(1 - R) = \frac{E_t}{Z_t} \quad (36)$$

where E_i and E_t are the incident electric field and transmitted electric field, respectively, and where $Z_0 = \sqrt{\mu_0/\epsilon_0}$ and $Z_t = \sqrt{\mu_0/\epsilon_t}$ are the characteristic impedances of free-space and object regions, respectively. From Eqs. (35) and (36), we can get the transmitted power:

$$\frac{|E_i|^2}{Z_0}(1 + R)(1 - R^*) = \frac{|E_t|^2}{Z_t^*}. \quad (37)$$

Taking the real part of Eq. (37), noting that $(1 + R)(1 - R^*) = 1 + R - R^* - RR^*$, and that $R - R^*$ is purely imaginary, we get

$$\text{Re} \left\{ \frac{|E_i|^2}{2Z_0}(1 - |R|^2) \right\} = \text{Re} \left\{ \frac{|E_t|^2}{2Z_t^*} \right\}. \quad (38)$$

We note that $Z_t = Z_0/\sqrt{\epsilon}$; $\epsilon = (n' + in'')^2$; $\epsilon' = n'^2 - n''^2$; $\epsilon'' = 2n'n''$; and we get

$$\frac{|E_i|^2}{2Z_0}(1 - |R|^2) = \text{Re} \left\{ \frac{|E_t|^2}{2Z_0} n' \right\} = \frac{|E_t|^2}{2Z_0} n'. \quad (39)$$

Using the expression for L_a in Eq. (18), and evaluating Eq. (34) at, $d \rightarrow \infty$ we get

$$\int_0^\infty \frac{\omega\epsilon_0\epsilon''}{2} |E_t|^2 \exp(-\alpha_2 z) dz = \frac{\omega\epsilon_0\epsilon''}{2} |E_t|^2 \frac{1}{\alpha_2} = \frac{|E_t|^2}{2Z_0} n', \quad (40)$$

where $\alpha_2 = k_0 2n''$ and $\epsilon'' = 2n'n''$.

Whereas the expression for transmitted power in Eq. (39) is derived from conservation of power and object interface boundary conditions, the expression for transmitted power in Eq. (40) is the total sum of the position dependent transmitted power given by Eq. (18). We can see that for objects where no energy transits the thickness of the object (i.e., object is thick relative to optical skin depth), these are equivalent.

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